

NAME: \_\_\_\_\_

1. Solve the following initial value problems.

(a)  $\frac{dN}{dt} = \frac{t+2}{t}$  for  $t \geq 1$  with  $N(1) = 2$ .

(b)  $\frac{dy}{dx} = \frac{e^{-x} + e^x}{2}$  for  $x \geq 0$  with  $y(0) = 0$ .

2. Approximate the area under the parabola  $y = x^2$  from 0 to 1 using four equal subintervals.

3. Use Leibniz's Rule to solve  $y = \frac{d}{dx} \int_x^{2x} (1+t^2)dt$ .

4. Find the average value of  $f(x) = -x^2 - 2x + 5$  over the interval  $[-4, 0]$ .

5. Find the area of the region bounded by  $y = x^2 + 1$  and  $y = x + 1$ .
6. Find the volume of the solid bounded by  $y = -x^2 + 1$ ,  $y = 0$ , and rotated about the x-axis
7. Imagine stacking squares whos sides are the length between  $f(x) = 2x^2 - 1$  and  $g(x) = 7$ . This would create a shape over the area between  $f(x)$  and  $g(x)$ . What is the volume of this solid?
8. Solve the indefinite integral  $\int x^3 e^{x^2} dx$ .