

NAME: \_\_\_\_\_

Problem 1. Find the general solutions for the following differential equations

$$\text{a) } \frac{dy}{dx} = \frac{3}{x^2} - 2x^2$$

$$\text{b) } \frac{dy}{dx} = \frac{1 + 2x}{x}$$

$$\text{c) } \frac{dy}{dx} = \frac{1}{1 + 2x}$$

$$\text{d) } \frac{dy}{dx} = \sec^2(3x - 1)$$

$$\text{e) } \frac{dy}{dx} = \frac{1}{x \ln(2x)} \quad [\text{Hint: consider } \frac{dy}{dx} \ln(\ln(x)).]$$

Problem 2. Solve the initial value problem that models the growth of a population with time:

$$\frac{dN}{dt} = t$$

where  $N(0) = 20$ .

Problem 3. Solve the initial value problem

$$\frac{dy}{dx} = -2x^2 + 3$$

where  $y(3) = 10$ .

Problem 4. An object moves with a constant acceleration of  $12 \text{ m/s}^2$ . Find the how far the object has fallen after 2 seconds if the object has the initial velocity  $v(0) = 4 \text{ m/s}$  and initial displacement of  $d(0) = 2 \text{ m}$ .